

## outline

<u>Topic</u>	<u>Reading</u>
• I Special relativity (4 lectures)	
• 1 Historical origins, postulates and spacetime	§ 2.1 – .13 (14)
• The tension between Newton and Maxwell	
• Postulates and assumptions of special relativity	
• Simultaneity and spacetime	
• 2 Relativistic kinematics	§ 3.1 – .6, .10 (10)
• The Minkowski metric	
• Lorentz transformations	
• Kinematic effects	
• 3 Relativistic dynamics	§ 3.7; 4.1 – .5 (12)
• Accelerated motion	
• Scalar and vector forces	
• Energy and momentum	
• 4 Non-Inertial motion and the equivalence principle	§ 3.8 – .9; 9.1 – .4 (14)
• Uniformly accelerated observers	
• Machian theories and equivalence	
• What is gravity?	
• II A crash course on Riemannian geometry (3 lectures)	
• 1 Differentiable manifolds	§ 5.1 – .9; 6.1, .2 (17)
• Manifolds and smooth functions	
• Vector and tensor fields	
• Mappings of manifolds and the Lie derivative	
• 2 Riemannian geometry	§ 6.3 – .12; 7.7 (18)
• Affine connections and curvature	
• Metric geometry	
• Isometries	
• 3 Integration on manifolds	§ 7.1 – .4 (6) +
• Differential forms and integrals	
• Volume and the Hodge dual	
• The generalized Stokes theorem	
• III Foundations of general relativity (6 lectures)	
• 1 Minkowski spacetime as a particular gravitational field	§ 7.5 – .6; 8.1 – .8 (18)
• A geometric perspective on special relativity	
• Geodesics and mechanics	
• Symmetry and conservation laws	
• 2 Gravity as geometry	§ 9.5 – .7; 10.1 – .7 (13)
• Tidal forces and geodesic deviation	
• The Einstein field equation	

<u>Topic</u>	<u>Reading</u>
<ul style="list-style-type: none"> <li>• Uniqueness of Einstein's theory</li> </ul>	
<ul style="list-style-type: none"> <li>• 3 Gravitational sources <ul style="list-style-type: none"> <li>• Matter sources</li> <li>• Einstein–Maxwell theory</li> <li>• Energy conditions</li> </ul> </li> </ul>	§ 12.1 – .8 (11)
<ul style="list-style-type: none"> <li>• 4 The nature of the field equations <ul style="list-style-type: none"> <li>• Constraints and gauge</li> <li>• The Cauchy problem</li> <li>• The cosmological constant</li> </ul> </li> </ul>	§ 13.1 – .7 (11)
<ul style="list-style-type: none"> <li>• 5 Motion in curved spacetime <ul style="list-style-type: none"> <li>• The Newtonian limit</li> <li>• The post-Minkowski expansion</li> <li>• <i>Does the field equation predict source motion?</i></li> </ul> </li> </ul>	§ 12.9, .10; 20.1, .2 (8) +
<ul style="list-style-type: none"> <li>• 6 *Action principles for gravity <ul style="list-style-type: none"> <li>• The Einstein–Hilbert action</li> <li>• The Palatini action</li> <li>• Coordinate invariance</li> </ul> </li> </ul>	§ 11.1 – .8 (9)
<ul style="list-style-type: none"> <li>• IV Isolated gravitational sources (6 lectures) <ul style="list-style-type: none"> <li>• 1 The Schwarzschild solution <ul style="list-style-type: none"> <li>• Stationary and static metrics</li> <li>• Spherical symmetry</li> <li>• Solving the Einstein equation</li> </ul> </li> </ul> </li> </ul>	§ 14.1 – .6 (10)
<ul style="list-style-type: none"> <li>• 2 Signatures of relativistic gravity <ul style="list-style-type: none"> <li>• Perihelion advance</li> <li>• Deflection of light</li> <li>• Gravitational red shift</li> </ul> </li> </ul>	§ 15.1 – .5 (13)
<ul style="list-style-type: none"> <li>• 3 The Schwarzschild black hole <ul style="list-style-type: none"> <li>• Singularities of the Schwarzschild solution</li> <li>• Eddington–Finkelstein coordinates</li> <li>• The event horizon</li> </ul> </li> </ul>	§ 16.1 – .8 (12)
<ul style="list-style-type: none"> <li>• 4 Global structure of the Schwarzschild solution <ul style="list-style-type: none"> <li>• The Kruskal extension</li> <li>• Conformal compactification</li> <li>• Penrose diagrams</li> </ul> </li> </ul>	§ 17.1 – .5 (9)
<ul style="list-style-type: none"> <li>• 5 *Spherical stars <ul style="list-style-type: none"> <li>• Interior solutions in spherical symmetry</li> <li>• Hydrostatic equilibrium</li> <li>• The Chandrasekhar limit</li> </ul> </li> </ul>	+
<ul style="list-style-type: none"> <li>• 6 *Rotating black holes <ul style="list-style-type: none"> <li>• The Kerr metric</li> <li>• Spacetime structure</li> </ul> </li> </ul>	§ 19.3 – .10 (12)

Topic	Reading
<ul style="list-style-type: none"> <li>• Maximal rotation</li> <li>• 7 *General features of black holes               <ul style="list-style-type: none"> <li>• What is a black hole?</li> <li>• Singularity and uniqueness theorems</li> <li>• Quantum effects</li> </ul> </li> </ul>	§ 18.1 – .5; 19.11 – .12 (13)
<ul style="list-style-type: none"> <li>• V Gravitational radiation (5 lectures)</li> </ul>	
<ul style="list-style-type: none"> <li>• 1 Plane gravitational waves               <ul style="list-style-type: none"> <li>• Plane waves in linearized gravity</li> <li>• Exact plane-wave solutions</li> <li>• Detecting gravitational waves</li> </ul> </li> </ul>	§ 20.3 – .5, .9 (12)
<ul style="list-style-type: none"> <li>• 2 Weak gravitational waves from compact sources               <ul style="list-style-type: none"> <li>• Radiation gauge in linearized gravity</li> <li>• Sources of gravitational radiation</li> <li>• The quadrupole formula</li> </ul> </li> </ul>	+
<ul style="list-style-type: none"> <li>• 3 Asymptotic description of gravitational radiation               <ul style="list-style-type: none"> <li>• Radiation coordinates</li> <li>• Characteristic formulation of general relativity</li> <li>• Bondi news</li> </ul> </li> </ul>	§ 21.1 – .6 (10)
<ul style="list-style-type: none"> <li>• 4 *Local characterization of gravitational radiation               <ul style="list-style-type: none"> <li>• Algebraic classification of metrics</li> <li>• The peeling-off theorem</li> <li>• Null congruences and propagation</li> </ul> </li> </ul>	§ 6.13; 21.7 – .9 (5) +
<ul style="list-style-type: none"> <li>• 5 *Radiation reaction in general relativity               <ul style="list-style-type: none"> <li>• The Dirac approach to radiation reaction</li> <li>• Second-order perturbation theory</li> <li>• Source motion and integrability</li> </ul> </li> </ul>	+
<ul style="list-style-type: none"> <li>• VI Relativistic cosmology (4 lectures)</li> </ul>	
<ul style="list-style-type: none"> <li>• 1 Homogeneous and isotropic spacetimes               <ul style="list-style-type: none"> <li>• The cosmological principle</li> <li>• Homogeneity and isotropy</li> <li>• Spaces of constant curvature</li> </ul> </li> </ul>	§ 22.1 – .8 (15)
<ul style="list-style-type: none"> <li>• 2 Basic cosmological phenomenology               <ul style="list-style-type: none"> <li>• The Friedmann equation</li> <li>• Observables in cosmology</li> <li>• Hubble's law</li> </ul> </li> </ul>	§ 22.9 – .12 (8)
<ul style="list-style-type: none"> <li>• 3 Simple cosmological models               <ul style="list-style-type: none"> <li>• The role of the cosmological constant</li> <li>• Classification of Friedmann solutions</li> <li>• Dark matter and dark energy</li> </ul> </li> </ul>	§ 23.1 – .10 (13)
<ul style="list-style-type: none"> <li>• 4 *Global structure of cosmological spacetimes               <ul style="list-style-type: none"> <li>• Cosmological horizons</li> </ul> </li> </ul>	§ 23.12 – .16 (11) +

**Topic****Reading**

- Conformal structure of cosmological solutions
- *Asymptotically simple spacetimes*
- 5 \*Quantum cosmology
- Symmetry reduction of the action
- Canonical quantization
- Relation to quantum gravity

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